

SOLUTIONS THEORY WITH ASSIGNMENT

TOPIC 1 : SOLUTIONS, EXPRESSING CONCENTRATION OF SOLUTIONS AND SOLUBILITY

1. A **solution** is a homogeneous mixture of two or more chemically non-reacting substances. Its composition can be varied within certain limits. All particles in a solution are generally of molecular size, i.e., 0.2 – 2nm. The components of a solution generally cannot be separated by filtration, settling or centrifuging.
2. A solution consists of two components: solute and solvent.
 - a. The component which is present in larger proportion is termed as the **solvent**. It is usually in the same physical state as the solution.
 - b. The component which is present in smaller proportion is called the **solute**.
3. A solution may be classified as solid, liquid or a gaseous solution. The different types of solutions along with examples are summarised below:

Types of Solution	Examples
Gaseous solution (a) Gas in gas (b) Liquid in gas (c) Solid in gas	Air, mixture of oxygen and nitrogen, etc. Water vapour. Camphor vapours in nitrogen gas.
Liquid solution (a) Gas in liquid (b) Liquid in liquid (c) Solid in liquid	Carbon dioxide dissolved in water (aerated water) oxygen dissolved in water, etc. Ethanol dissolved in water, vinegar, formalin, etc. Sugar dissolved in water, saline water, etc.
Solid solutions (a) Gas in solid (b) Liquid in solid (c) Solid in solid	Solution of hydrogen in palladium. Amalgams, eg., sodium amalgam. Gold ornaments (copper or silver dissolved in gold).

4. **Methods of expressing concentrations of solution**
 - a. **Mass percentage:** It is the amount of solute in grams present in 100g of solution.

$$\text{Mass percent of solute} = \frac{\text{Mass of solute}}{\text{Mass of solution}} \times 100$$

- b. **Molarity** = It is defined as the number of moles of solute present in one litre of solution.

$$\text{Molarity (M)} = \frac{\text{Number of moles of solution}}{\text{Volume of solution in litre}} = \frac{n}{v} \quad ; \quad n = \frac{\text{Weight in grams}}{\text{Molecular weight of solute}}$$

$$\therefore M = \frac{\text{Weight in grams}}{\text{Volume of solution in litres}} \times \frac{1}{\text{Molecular weight of solute}}$$

Strength: This is weight (in gms) of solute per litre of solution

$$\therefore \text{Strength} = \text{Molarity} \times \text{Molecular weight}$$

or $\text{Strength} = \text{Molarity} \times \text{Molecular weight}$

Note: Molarity is the most common way of expressing concentration of a solution in laboratory. However, it has one disadvantage. It changes with temperature because volume of a solution alters due to expansion and contraction of the liquid with temperature.

c. Molality: It is defined as the number of moles of a solute present in 1000g (1 kg) of a solvent.

$$\text{Molality (m)} = \frac{\text{Number of moles of solute}}{\text{Weight of solvent in kg}} = \frac{n}{W}$$

Note: Molality is considered better way of expressing concentration of solutions as compared to molarity because molarity does not change with change in temperature since the mass of solvent does not vary with temperature.

d. Volume percentage: It is the volume of solute in cm³ present in 1000 cm³ of solution.

$$\text{Volume percent of solute} = \frac{\text{Volume of solute}}{\text{Volume of solution}} \times 100$$

e. Parts per million: When a solute is present in trace quantities it is convenient to express concentration in parts per million (ppm).

$$\text{Parts per million} = \frac{\text{Number of parts of solute}}{\text{Total number of parts of all components of the solution}} \times 10^6$$

f. Mole fraction: It is defined as the ratio of the number of moles of the solute to the total number of moles in the solution. If n_A is the number of moles of solute dissolved in n_B moles of solvent, then

$$\text{Mole fraction of solute } (X_A) = \frac{n_A}{n_A + n_B} \quad \dots (1)$$

$$\text{Mole fraction of solvent } (X_B) = \frac{n_B}{n_A + n_B} \quad \dots (2)$$

Adding the above two equations, we get

$$X_A + X_B = \frac{n_A}{n_A + n_B} + \frac{n_B}{n_A + n_B} = \frac{n_A + n_B}{n_A + n_B} = 1$$

i.e.,

$$X_A + X_B = 1$$

∴

$$X_A = 1 - X_B \text{ or } X_B = 1 - X_A$$

Note: Even if three components make a solution, then $X_A + X_B + X_C = 1$.

5. Solubility: It is defined as the amount of solute in a saturated solution per 100g of a solvent. Solubility is guided by general principle of like dissolves like.

Ionic and polar substances are generally soluble in polar solvents like water and are insoluble in non-polar solvents like benzene, chloroform, carbon disulphide, etc.

Similarly, non-polar solutes like 'iodine', sulphur, phosphorus and organic substances are soluble in non-polar solvents like benzene, chloroform, etc., and are insoluble in polar solvents like water.

6. The solubility of a gas in a liquid depends upon

- a. the nature of the gas and the nature of the liquid,
- b. the temperature of the system, and
- c. the pressure of the gas.

7. The solubility of a gas in a given liquid varies considerably with the nature of the gas.

a. Generally, the gases which can be easily liquefied are more soluble in common solvents. For example, CO₂ is more soluble in water as compared to oxygen or nitrogen.

b. The gases which are capable of forming ions in aqueous solution are much more soluble in water than in any other solvent. For example, HCl and NH₃ are highly soluble in water in which they form ions but not in benzene.

c. The solubility of a gas in a liquid decreases with rise in temperature of the solution.

d. The effect of pressure on the solubility of a gas in a liquid is governed by Henry's Law. It states that the solubility of a gas in a liquid at a given temperature is directly proportional to the partial pressure of the gas. Mathematically, $P = K_H X$

where P is the partial pressure of the gas; and X is the mole fraction of the gas in the solution and K_H is Henry's Law constant.

8. Applications of Henry's law :

- To increase the solubility of CO_2 in soft drinks and soda water, the bottle is sealed under high pressure.
- Scuba divers much cope with high concentrations of dissolved gases while breathing air at high pressure under water. Increased pressure increases the solubility of atmospheric gases in blood. When the divers come towards surface, the pressure gradually decreases. This releases two dissolved gases and leads to the formation of bubbles of nitrogen in the blood. This blocks capillaries and creates a medical condition known as bends, which are painful and dangerous to life. To avoid bends, as well as, the toxic effects of high concentrations of nitrogen in the blood, the tanks used by scuba divers are filled with air diluted with helium (11.7% helium, 56.2% nitrogen and 32.1% oxygen).
- At high attitudes, the partial pressure of oxygen is less than that at the ground level. This leads to low concentrations of oxygen in the blood and tissues of people living at high altitudes or climbers low blood oxygen causes climbers to become weak and unable to think clearly, symptoms of a condition known as anoxia.

ILLUSTRATIONS

- If the density of some lake water is 1.25 g mL^{-1} and it contains 92 g of Na^+ ions per kg of water. Calculate the molality of Na^+ ions in the lake.

Sol. Number of moles in 92 g of Na^+ ions = $\frac{\text{Mass}}{\text{Molecular mass}} = \frac{92}{23} = 4 \text{ mol}$

$$\text{Molality of } \text{Na}^+ \text{ ions} = \frac{\text{Number of moles}}{\text{Mass of solvent (kg)}} = \frac{4}{1} = 4 \text{ mol kg}^{-1}$$

- If the solubility product of CuS is 6×10^{-16} , calculate the maximum molarity of CuS in aqueous solution.

Sol. Maximum molarity of CuS in aqueous solution is the solubility (s) in mol L^{-1} .



$$\therefore s^2 = 6 \times 10^{-16} \quad (\text{Given}) \quad \therefore s = \sqrt{6 \times 10^{-16}} = 2.45 \times 10^{-8} \text{ mol L}^{-1}$$

- Calculate the mass of urea (NH_2CONH_2) required in making 2.5 kg of 0.25 molal aqueous solution.

Sol. Since, the molal aqueous solution of urea is 0.25 m. \therefore Moles of urea = 0.25 mol and

Mass of solvent (water) = 1 kg = 1000 g

Molar mass of urea (NH_2CONH_2) = $14 + 2 + 12 + 16 + 14 + 2 = 60 \text{ g mol}^{-1}$;

\therefore 0.25 mole of urea = $0.25 \text{ mole} \times 60 \text{ g mol}^{-1} = 15 \text{ g}$; Total mass of solution = $1000 + 15 \text{ g} = 1015 \text{ g} = 1.015 \text{ kg}$

Thus, 1.015 kg of solution contains urea = 15 g; \therefore 2.5 kg of solution will require urea

$$= \frac{15 \text{ g}}{1.015 \text{ kg}} \times 2.5 \text{ kg} = 37 \text{ g}$$

- Will the molarity of a solution at 50°C be same, less or more than at 25°C ?

Sol. Molarity at 50°C will be less than that at 25°C , because molarity decreases with increase in temperature.

Since, volume of the solution increases with increase in temperature but number of moles of solute remains the same.

PRACTICE PROBLEMS

- State Henry's law. What is the effect of temperature on the solubility of a gas in a liquid?
- A solution of glucose in water is labelled as 10% w/w. What would be the molality and mole fraction of each component in the solution? If the density of the solution is 1.2 g mL^{-1} , then what shall be the molarity of the solution?
- Why do smaller particles dissolve faster than larger ones?
- Define the term solution. How many types of solutions are formed? Write briefly about each type with an example.

TOPIC 2 : VAPOUR PRESSURE OF LIQUID SOLUTIONS

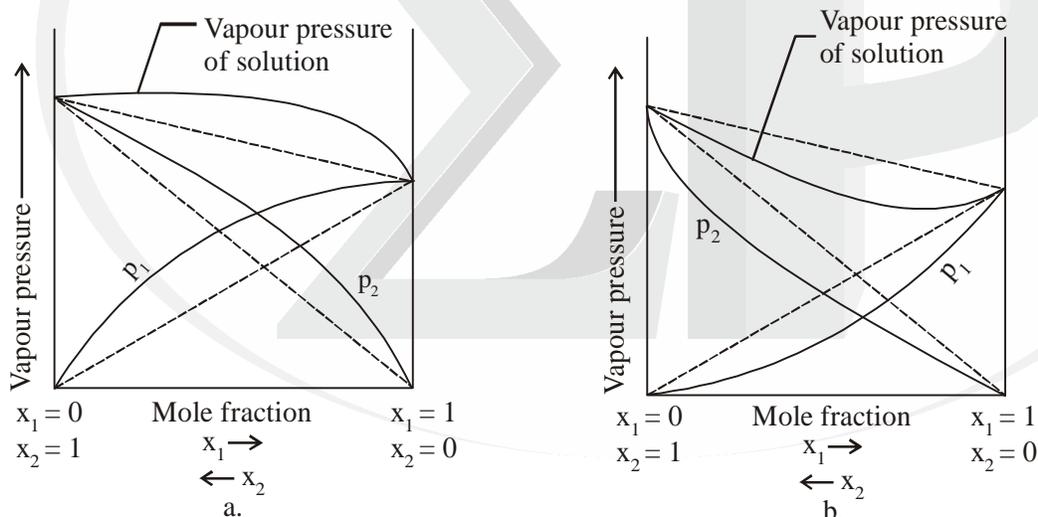
- The **vapour pressure** of a liquid is the pressure exerted by its vapour when it is in dynamic equilibrium with its liquid, in a closed container.
- When a non-volatile solute is added to a solvent to make a solution, the vapour pressure of the solutions will be the vapour pressure of the solvent as there is no contribution from the solute.
- According to **Raoult's Law**, the vapour pressure of a solution containing a non-volatile solute is directly proportional to the mole fraction of the solvent (X_A). The proportionality constant being the vapour pressure of the pure solvent, i.e., $P \propto X_A$ or $P = P^0 X_A$.
If the solution consists of two volatile liquids, then Raoult's Law is applicable to each component of the solution, i.e.,

$$P_A = P_A^0 X_A \text{ and } P_B = P_B^0 X_B$$

The total vapour pressure of the solution is equal to the sum of the partial pressures of each component

$$P = P_A + P_B = P_A^0 X_A + P_B^0 X_B$$

- A solution which obeys Raoult's Law at all concentrations and temperatures is known as an **ideal solution**.
 - Characteristics of an ideal solution:
 - It obeys Raoult's Law at all concentrations and temperature.
 - $\Delta_{\text{sol}} H = 0$; i.e., there is no change in volume when an ideal solution is formed.
 - $\Delta_{\text{sol}} H = 0$; i.e., heat is neither evolved nor absorbed during the formation of an ideal solution.
 - Solutions which do not obey Raoult's Law are known as **non-ideal solutions**.
 - The vapour pressure of a non-ideal solution is either higher or lower than that predicted by Raoult's Law.
 - The solution shows **positive deviation** from Raoult's Law if its vapour pressure is higher than that predicted by Raoult's Law.
 - The solution shows **negative deviation** if its vapour pressure is lower than that predicted by Raoult's Law.
- It is important to know the graphical representations of ideal, positive deviating and negative deviating solutions. These are given below:



The ideal or non ideal behaviour of solutions depends on solvent-solute interactions. Let A represent the solvent and B represent the solute then we can write it as

- If $A - B$ interactions = $A - A$ & $B - B$ then we get ideal solution.
 - If $A - B$ interactions $>$ $A - A$ & $B - B$ then we get solution showing negative deviation having $\Delta_{\text{sol}} V < 0$ & $\Delta_{\text{sol}} H^\circ > 0$.
 - If $A - B$ interactions $<$ $A - A$ & $B - B$ then we get solⁿ showing +ve deviation having $\Delta_{\text{sol}} V > 0$ & $\Delta_{\text{sol}} H^\circ > 0$.
- According to Raoult's Law, the vapour pressure of volatile component in a given solution is given by

$$P_A = P_A^0 X_A \quad \dots(i)$$

According to Henry's Law, the solubility of a gas (volatile component) in a liquid is governed by the expression.

$$P = K_H X \quad \dots(\text{ii})$$

Note:

a. It can be seen from equations (i) and (ii) that the partial pressure of the volatile component or gas is directly proportional to its mole fraction in the solution. Only the proportionality constant K_H , in the Henry's Law equation, differs from P_A° , the proportionality constant in Raoult's Law equation.

b. If K_H becomes equal to P_A° , the Raoult's Law becomes a special case of Henry's Law.

8. In a very dilute solution of liquids, the solvent obeys Raoult's Law whereas the solute obeys Henry's Law.

ILLUSTRATIONS

1. Two liquids A and B boil at 155°C and 190°C, respectively. Which of them has a higher vapour pressure at 80 °C?

Sol. A is more volatile, therefore has higher vapour pressure.

2. What type of deviation is shown by a mixture of ethanol and acetone? Give reason.

Sol. A mixture of ethanol and acetone shows positive deviation because in this case, A—B interactions are weaker than A—A and B—B interactions. Due to this, vapour pressure increases which results in positive deviation.

3. At some temperature, the vapour pressure of pure C_6H_6 is 0.2456 bar and that of pure $C_6H_5CH_3$ (toluene) is 0.0925 bar. If the mole fraction of toluene in solution is 0.6. Then,

(i) what will be the total pressure of the solution? (ii) what will be the mole fraction in vapour phase?

Sol. (i) According to Raoult's law, $p_1 = p_1^\circ \times \chi_1$; For toluene, $p_1^\circ = 0.09256$ bar and $\chi_1 = 0.6$

Then, $p_1 = 0.925 \times 0.6 = 0.0555$ bar; For benzene, $p_2 = p_1^\circ \times \chi_2$; Mole fraction of benzene,

$\chi_2 = 1 - \chi_1 = 1 - 0.6 = 0.4$ and $p_2^\circ = 0.256$ bar; Then $p_2 = 0.256 \times 0.4 = 0.1024$ bar

Total vapour pressure of solution; $p_{\text{total}} = p_1 + p_2 = 0.1024 + 0.0555 = 0.158$ bar

(ii) Mole fraction of benzene in vapour phase $y_2 = \frac{p_2}{p_{\text{total}}} = \frac{0.1024}{0.158} = 0.648$

4. Benzene and toluene both have equal mole fractions in their mutual solution. What do you expect about their mole fraction in vapour phase at the same temperature. (Given, $p_{\text{benzene}}^\circ = 3p_{\text{toluene}}^\circ$)

Sol. $\therefore \chi_B = \chi_T$ [mole fractions are equal] $\therefore \frac{p_B}{p_T} = \frac{p_B^\circ}{p_T^\circ}$ But given that $\frac{p_B^\circ}{p_T^\circ} = 3 \therefore \frac{p_B}{p_T} = 3$

But $\frac{p_B}{p_T} = 3$ shows that $\frac{y_B}{y_T} = 3$ in vapour phase, since vapour pressures in vapour phase are in the ratio of their number of moles or mole fraction.

PRACTICE PROBLEMS

1. Two liquids x and y on mixing form an ideal solution. The vapour pressure of a solution containing 3 moles of x and 1 mole of y is 550 mm Hg. However, when 4 moles of x and 1 mole of y are mixed, the vapour pressure of solution thus formed is 560 mm Hg. What will be the vapour pressure of pure x and pure y at this temperature?

OR

Two liquids A and B form an ideal solution. At 300 K, the vapour pressure of a solution containing 1 mole of A and 3 moles of B is 550 mm of Hg. At the same temperature, if one more mole of B is added to this solution, the vapour pressure of the solution increases by 10 mm of Hg. Determine the vapour pressure of A and B in their pure states.

- An aqueous solution containing 28% by mass of a liquid A (mol. mass = 140) has a vapour pressure of 160 mm at 37°C. Find the vapour pressure of the pure liquid A. (The vapour pressure of water at 37°C is 150 mm)
- Methanol and ethanol form nearly ideal solution at 300 K. A solution is made by mixing 32 g methanol and 23 g ethanol at 300 K. Calculate the partial pressures of its constituents and the total pressure of the solution.
- Vapour pressure of two liquids A and B are 120 and 180 mm Hg at a given temperature. If 2 mole of A and 3 mole of B are mixed to form an ideal solution, calculate the vapour pressure of solution at the same temperature.
- The vapour pressure of pure liquid A and pure liquid B at 20°C are 22 and 75 mm Hg respectively. A solution is prepared by mixing equal moles of A and B. Assuming the solution to be ideal, calculate the vapour pressure of the solution.

TOPIC 3 :

- Colligative properties** of solutions are those properties which depend only upon the number of solute particles in the solution and not on their nature. Such properties are
 - Relative lowering in vapour pressure,
 - Elevation of boiling point,
 - Depression of freezing point and
 - Osmotic pressure.
- According to Raoult's Law, the vapour pressure of a solution containing a non-volatile solute is given by

$$P = P_A = P_A^\circ X_A$$

$$\text{Lowering of vapour pressure} = P_A^\circ - P_A = P_A^\circ - P_A^\circ X_A \quad ; \quad P_A^\circ - P_A = P_A^\circ (1 - X_A)$$

$$\text{Since for a binary mixture, } X_A + X_B = 1 \quad X_B = 1 - X_A \quad \therefore \quad P_A^\circ - P_A = P_A^\circ X_B$$

$$\text{Relative lowering of vapour pressure} = \frac{P_A^\circ - P_A}{P_A^\circ} \quad ; \quad \frac{P_A^\circ - P_A}{P_A^\circ} = X_B = \frac{n_B}{n_A + n_B}$$

Thus, according to Raoult's Law, the relative lowering of vapour pressure of a solution is equal to the mole fraction of the solute.

$$\text{For a very dilute solution, } \frac{n_B}{n_A + n_B} \approx \frac{n_B}{n_A} \quad ; \quad \therefore \quad \frac{P_A^\circ - P_A}{P_A^\circ} = \frac{n_B}{n_A} = \frac{W_B/M_B}{W_A/M_A} = \frac{W_B M_A}{M_B W_A}$$

- The **boiling point** of a liquid is the temperature at which the vapour pressure of the liquid becomes equal to the atmospheric pressure. When a non-volatile solute is dissolved in a solvent, its vapour pressure decreases as there is no contribution from the non-volatile solute. Therefore, the boiling point of the solution is always higher than the boiling point of the pure solvent.

For a dilute solution, the elevation in boiling point is found to be proportional to the molality of the solution, i.e., $\Delta T_b \propto m$ or $\Delta T_b = K_b m$

where ΔT_b is the elevation in boiling point, 'm' is the molality of K_b is the Molal elevation constant (boiling elevation constant) which is equal to the elevation in boiling point when one mole of the solute is dissolved in 1000g of the

$$\text{solvent.} \quad \Delta T_b = K_b \frac{n_B}{W_A (g)} \times 1000 \quad \Delta T_b = 1000 \frac{K_b W_B}{M_B W_A}$$

- Freezing point** is the temperature at which the solid and the liquid state of the substance have the same vapour pressure. Since the presence of a non-volatile solute lowers the vapour pressure of the solvent, the freezing point of the solution is always less than that of the pure solvent. The depressions in freezing point (ΔT_f) is proportional to the molality of the solution.

$$\Delta T_f \propto m \quad \text{or} \quad \Delta T_f = K_f m$$

where K_f is **molal depression constant** (freezing point depression constant). It is the depression in freezing point when 1 mole of a solute is dissolved in 1000 g of the solvent

$$\Delta T_f = 1000 K_f \frac{W_B}{W_A M_B}$$

5. The spontaneous flow of solvent molecules from a dilute solution into a concentrated solution when the two are separated by a perfect semipermeable membrane is called osmosis.
6. **Osmotic pressure** (π) is the pressure which must be applied to the solution side (more concentrated solution) to just prevent the passage of pure solvent into it through a semipermeable membrane.

Mathematically, $\pi = CRT = \frac{n_B}{V} RT$ where π is the osmotic pressure of the solution,

C is the concentration of solution ; n_B is the number of moles of solute,

V is the volume of the solution in litres, ; R is the gas constant, and

T is the temperature on the Kelvin scale.

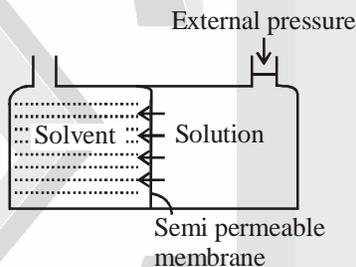
while solving the problems, we have to take proper care of units. If π is in atm, then R should be taken as $0.083 \text{ lit atm mol}^{-1}\text{K}^{-1}$.

7. **Isotonic solutions** are those solutions which have the same osmotic pressure. Also they have same molar concentration.

For isotonic solutions, $p_1 = p_2$ Also $C_1 = C_2$ or $\frac{n_1}{V_1} = \frac{n_2}{V_2}$ $\frac{W_1}{m_1 V_1} = \frac{W_2}{m_2 V_2}$

8. When two solutions have different osmotic pressures, the solution of lesser osmotic pressure is called **hypotonic solutions** and the solutions of higher osmotic pressure is called hypertonic solutions.

9. The movement of solvent particles from higher concentration to lower concentration through semipermeable membrane on applying pressure is known as **reverse osmosis**. If the external pressure greater than osmotic pressure is applied on more concentrated solution side, the solvent molecules start passing through semipermeable membrane from this solution to the solvent or less concentrated solution. This is known as reverse osmosis. It is used to purify the sea water.



ILLUSTRATIONS

1. Calculate the boiling point of a solution containing 1.8 g of a non-volatile solute dissolved in 90 g of benzene. The boiling point of pure benzene is 353.23 K. [$K_b = 2.53 \text{ K kg mol}^{-1}$ and molar mass of solute = 58 g mol^{-1}]

Sol. For boiling point elevation, we can use the relation, $\Delta T = K_{b1000} \times \frac{w_B \times 1000}{m_B \times w_A}$

Given: $K_b = 2.53 \text{ K kg mol}^{-1}$; $w_B = 1.8 \text{ g}$; $m_B = 58$; $w_A = 90 \text{ g}$.

$$\therefore \Delta T = 2.53 \times \frac{1.8 \times 1000}{58 \times 90} = 0.87 \text{ K}; \quad T = T_0 + 0.87 = 353.23 + 0.87 = 354.1 \text{ K}$$

2. The boiling point of water (100°C) becomes 100.52°C if 3 g of a non-volatile solute is dissolved in 20 mL of it. Calculate the molar mass of the solute. (K_b for water = 0.52 K m^{-1})

Sol. $m_B = \frac{1000 \times K_b \times w_B}{\Delta T \times w_A}$; Given: $K_b = 0.52 \text{ K m}^{-1}$; $w_B = 3 \text{ g}$; $w_A = 20 \times 1 = 20 \text{ g}$;

$$\Delta T = 100.52 - 100.0 = 0.52 \text{ K}; \quad \text{Putting these values in the above formula, } m_B = \frac{1000 \times 0.52 \times 3}{0.52 \times 20} = 150$$

3. An aqueous solution freezes at -0.186°C . Find its elevation in boiling point. $K_f = 1.86 \text{ K m}^{-1}$, $K_b = 0.512 \text{ K m}^{-1}$

Sol. $\Delta T = K_f \times m$; $0.186 = 1.86$; $m = 0.1$; The elevation in boiling point of solution can be calculated as
 $\Delta T = K_b \times m = 0.512 \times 0.1 = 0.0512$

4. Calculate the temperature at which a solution containing 54 g of glucose, $\text{C}_6\text{H}_{12}\text{O}_6$, in 250 g of water will freeze. (K_f for water = $1.86 \text{ K kg mol}^{-1}$)

Sol. We know, $\Delta T = K_f \times \frac{w_B \times 1000}{m_B \times w_A}$ (i)

Given: $K_f = 1.86 \text{ K kg mol}^{-1}$, $w_B = 54 \text{ g}$, $w_A = 250 \text{ g}$; $m_B = 180 \text{ g/mol}$ (molar mass of glucose)

Putting these values in eqn. (i) we get, $\Delta T = 1.86 \times \frac{54 \times 1000}{180 \times 250} = 2.232$; $T_0 - T = 2.232$; $273 - T = 2.232$;

$T = 273 - 2.232 = 270.768 \text{ K}$ or -2.232°C

5. The osmotic pressure of a solution of an organic substance containing 18 g in one litre of solution at 293 K is $2.414 \times 10^5 \text{ N m}^{-2}$. Find the molecular mass of the substance if $S = 8.3 \text{ J K}^{-1} \text{ mol}^{-1}$.

Sol. Applying the equation; $\pi V = \frac{w_B}{m_B} \cdot ST$ or $m_B = \frac{w_B}{\pi V} \cdot ST$

Given: $\pi = 2.414 \times 10^5 \text{ Nm}^{-2}$, $V = 1.0 \text{ litre} = 1 \times 10^{-3} \text{ m}^3$, $S = 8.3 \text{ J K}^{-1} \text{ mol}^{-1}$, $w_B = 18 \text{ g}$ and $T = 293 \text{ K}$

$$m_B = \frac{18}{2.414 \times 10^5 \times 1 \times 10^{-3}} \times 8.3 \times 293 = 181.33$$

6. A solution containing 15 g urea (molar mass = 60 g mol^{-1}) per litre of solution in water has the same osmotic pressure (isotonic) as a solution of glucose (molar mass = 180 g mol^{-1}) in water. Calculate the mass of glucose present in one litre of its solution.

Sol. Glucose and urea are non-electrolytes hence their solutions must have same molarity for the solutions to be isotonic.

$$\left(\frac{w_B \times 1000}{m_B \times V} \right)_{\text{urea}} = \left(\frac{w_B \times 1000}{m_B \times V} \right)_{\text{glucose}}; \quad \frac{15 \times 1000}{60 \times 1000} = \frac{w_B \times 1000}{180 \times 1000}; \quad w_B = \frac{15 \times 180}{60} = 45 \text{ g}$$

\therefore 45 g glucose should be present in one litre of its solution.

PRACTICE PROBLEMS

1. Calculate the molal elevation constant of water of molar enthalpy of vaporisation of water at 373 K is $40.585 \text{ kJ mol}^{-1}$.
2. An aqueous solution of glucose boils at 100.02°C . What is the number of glucose molecules in the solution containing 100 g of water? (Given: K_b for $\text{H}_2\text{O} = 0.5 \text{ K m}^{-1}$; $N_A = 6.023 \times 10^{23}$)
3. The freezing point of cyclohexane is 279.65 K. A solution of 14.75 g of a solute in 500 g of cyclohexane has a freezing point of 277.33 K. Calculate the molar mass of the solute (given $K_f = 20.2 \text{ K kg mol}^{-1}$).
4. At 10°C , the osmotic pressure of urea solution was found to be 500 mm. The solution is diluted and temperature is raised to 25°C . When osmotic pressure was noticed to be 105.3 mm, determine the extent of dilution.
5. The osmotic pressure of a solution containing 30 g of a substance in 1 litre solution at 20°C is 3.2 atmosphere. Calculate the value of S. The molecular mass of the solute is 228.

TOPIC 4:

1. **Abnormal Molar Masses** As all the colligative properties are proportional to the number of moles, of solute, we can use them to calculate molecular weight of solutes (M_g). If the solute undergoes association or dissociation then the value of colligative property will give us abnormal molecular weight of solute. To correct this abnormal molecular weight van't Hoff factor i is used. Van't Hoff factor, ' i ' is used to express the extent of association or dissociation

of solutes in solution. It is the ratio of the normal and observed molar masses of the solute, i.e.,

$$i = \frac{\text{Normal molar mass}}{\text{Observed molar mass}} \quad \text{or} \quad i = \frac{\text{Calculated molar mass}}{\text{Experimental molar mass}}$$

- In case of association, observed molar mass being more than the normal, the factor 'i' has a value less than one. But in case of dissociation, the Van't Hoff factor is more than one because the observed molar mass has a less value.
- In case of solutes which do not undergo any association or dissociation in a solvent, the van't Hoff factor, 'i', will be equal to one because the observed and normal molar masses will be same.
- Molar mass $\propto \frac{1}{\text{Colligative property}}$

Therefore, van't Hoff factor may also be expressed as : $i = \frac{\text{Observed or calculated value of colligative property}}{\text{Normal or experimental value of colligative property}}$

- Inclusion of van't Hoff factor, 'i', modifies the equations for colligative properties as follows:
 Elevation in boiling point, $\Delta T_b = i K_b m$; Depression in freezing point, $\Delta T_f = i K_f m$
 Osmotic pressure, $\pi = i CRT$

ILLUSTRATIONS

- What mass of NaCl (molar mass = 58.5 g mol⁻¹) must be dissolved in 65 g of water to lower the freezing point by 7.5°C ? The freezing point depression constant, K_f for water is 1.86 K kg mol⁻¹. Assume van't Hoff factor for NaCl is 1.87.

Sol. We know, $\Delta T = i \times K_f \times \frac{w_B \times 1000}{m_B \times w_A}$ (i)

Given: $m_B = 58.5 \text{ g mol}^{-1}$; $w_A = 65 \text{ g}$; $i = 1.87$, $K_f = 1.86 \text{ K kg mol}^{-1}$; $\Delta T = 7.5$

Putting these values in eqn. (i) we get : $7.5 = 1.87 \times 1.86 \times \frac{w_B \times 1000}{58.6 \times 65}$; $w_B = 8.213 \text{ g} = 8.2 \text{ g}$

∴ Mass of NaCl to be dissolved in 8.2 g.

- Calculate the amount of KCl which must be added to 1 kg water so that the freezing point is depressed by 3 K.

Sol. We know, $\Delta T_{\text{obs}} = i K_f \times \frac{w_B \times 1000}{m_B \times w_A}$; where; i = van't Hoff factor = 2 for KCl

$K_f = 1.86 \text{ K m}^{-1}$ for water; $w_B = ?$; $m_B = 74.5$ (molar mass of KCl); $w_A = 1000 \text{ g}$; $\Delta T_{\text{obs}} = 3 \text{ K}$

Substituting these values in the above equation, we get $3 = 2 \times 1.86 \times \frac{w_B \times 1000}{74.5 \times 1000}$; $w_B = 60.08 \text{ g}$

- The freezing point of a solution containing 0.3 g ethanoic acid in 30 g of benzene is depressed by 0.45 K. Calculate the van't Hoff factor of ethanoic acid. What can you say about the nature of ethanoic acid in benzene? [$K_f(\text{C}_6\text{H}_6) = 5.12 \text{ K kg mol}^{-1}$; Molar mass of $\text{CH}_3\text{COOH} = 60 \text{ g mol}^{-1}$]

Sol. The van't Hoff factor can be calculated by using following relation

$$\Delta T = i \times K_f \times m; \quad \Delta T = i \times K_f \times \frac{w_B \times 1000}{m_B \times 1000} \quad \dots(i)$$

Given: $\Delta T = 0.45 \text{ K}$; $K_f = 5.12 \text{ K kg mol}^{-1}$; $w_B = 0.3 \text{ g}$, $w_A = 30 \text{ g}$; $m_B = 60 \text{ g mol}^{-1}$

Putting these values in eqn. (i), we get $0.45 = i \times 5.12 \times \frac{0.3 \times 1000}{60 \times 30}$; $i = 0.527$

Since, $i < 1$, hence ethanoic acid should be associated in benzene.

4. A $\frac{M}{10}$ solution of potassium ferrocyanide is 46% dissociated at 18°C. What will be its osmotic pressure?

Sol. We know, $\pi = iCST$ Given: $C = 0.1 \text{ M}$; $T = 18 + 273 = 291 \text{ K}$; $S = 0.0821 \text{ litre atm K}^{-1} \text{ mol}^{-1}$
Potassium ferrocyanide undergoes dissociation as, $K_4 [Fe(CN)_6] \rightleftharpoons 4K^+ + [Fe(CN)_6]^{4-}$; $n = 5$

$$\text{We know, } \alpha = \frac{i-1}{n-1}; \quad \alpha = \frac{46}{100} = 0.46; \quad 0.46 = \frac{i-1}{5-1}; \quad i = 2.84$$

From eqn. (i), $\pi = 2.84 \times 0.1 \times 0.0821 \times 291 = 6.785 \text{ atm}$

5. Decinormal solution of NaCl developed an osmotic pressure of 4.6 atmosphere at 300 K. Calculate its degree of dissociation ($S = 0.0821 \text{ litre atm K}^{-1} \text{ and mol}^{-1}$).

Sol. Given: $C = 0.1 \text{ M}$; $\pi = 4.6 \text{ atm}$; $T = 300 \text{ K}$; $S = 0.0821 \text{ litre atm K}^{-1} \text{ mol}^{-1}$

Substituting these values in the following equation, we can calculate van't Hoff factor.

$$i = \frac{\pi}{CST} = \frac{4.6}{0.1 \times 0.0821 \times 300} = 1.87; \quad \text{For dissociation, } \alpha = \frac{i-1}{n-1} \quad \text{for NaCl: } n = 2 = \frac{1.87-1}{2-1} = 0.87$$

\therefore % dissociation = 87

6. 0.5 g KCl was dissolved in 100 g water and the solution originally at 20°C, froze at -0.24°C. Calculate the percentage ionization of salt. (K_f per 1000 g of water = 1.86°C)

Sol. We know, $\Delta T = i \times K_f \times \frac{w_B \times 1000}{m_B \times w_A}$ (i) $\Delta T = 0.24$, $K_f = 1.86 \text{ Km}^{-1}$, $w_A = 100 \text{ g}$

$$w_B = 0.5 \text{ g}, m_B = 74.5. \quad \text{Putting these values in eqn. (i), we get } 0.24 = i \times 1.86 \times \frac{0.5 \times 1000}{74.5 \times 100}; \quad i = 1.922$$

$$\text{For KCl: } KCl \rightleftharpoons K^+ + Cl^- \quad (n = 2) \quad \alpha = \frac{i-1}{n-1} = \frac{1.922-1}{2-1} = 0.922$$

\therefore Percentage ionization of salt = $0.922 \times 100 = 92.2$

PRACTICE PROBLEMS

- Phenol associates in benzene to a certain extent to form a dimer. A solution containing $2 \times 10^{-2} \text{ kg}$ of phenol of 1 kg of benzene has its freezing point decreased by 0.69 K. Calculate the degree of association of phenol. (K_f for benzene = $5.12 \text{ K kg mol}^{-1}$).
- Calculate the amount of NaCl which must be added to 100 g of water, so that freezing point of water is depressed by 2K. ($K_f = 1.86 \text{ Km}^{-1}$) (Assume complete dissociation of NaCl)
- 2 g of benzoic acid (C_6H_5COOH) dissolved in 25 g of benzene shows a depression in freezing point equal to 1.62 K. Molal depression constant for benzene is $4.9 \text{ K kg mol}^{-1}$. What is the percentage association of the acid if it forms a dimer in solution?
- Arrange the following solutions in the increasing order of their osmotic pressures.
a. 34.2 g/litre sucrose b. 60 g/litre of urea c. 90 g/litre of glucose d. 58.5 g/litre of sodium chloride
Give reason in support of your answer.
- Benzoic acid completely dimerises in benzene. What will be the vapour pressure of solution containing 61 g benzoic acid per 500 g benzene when the vapour pressure of pure benzene at that temperature of experiment is 66.6 torr? What will be the vapour pressure in normal state.
- 0.5 g KCl was dissolved in 100 g water and the solution originally at 20°C, froze at -0.24°C. Calculate the percentage ionization of salt. ($K_f = 1.86 \text{ K kg mol}^{-1}$)
- Calculate the freezing point depression for 0.0711 m aqueous solution of Na_2SO_4 , if it is completely ionized in the solution. If this solution actually freezes at -0.32°C. What is the value of van't Hoff factor for it at freezing point? (K_f for water is $1.86 \text{ K kg mol}^{-1}$)

IMPORTANT TIPS

1. **Grams per litre:** It is defined as the amount of the solute in grams present in one litre of the solution. Concentration

$$\text{or strength of solution} = \frac{\text{Mass of solute in grams}}{\text{Volume of solution in litres}} = \frac{W}{V} \text{ g/litre.}$$

2. **Molarity of dilution:**

$$\begin{array}{ccc} \text{Before dilution} & & \text{After dilution} \\ M_1 V_1 & & M_2 V_2 \end{array}$$

3. **Molarity of mixing:** $M_1 V_1 + M_2 V_2 + M_3 V_3 = M_R (V_1 + V_2 + V_3)$

where M_R = Resultant molarity,

$V_1 + V_2 + V_3$ = Resultant volume after mixing.

4. **Normality:** It is defined as the number of gram equivalents of a solute dissolved in one litre of solution.

$$\text{Normality (N)} = \frac{\text{Number of gram equivalents of a solute}}{\text{Volume of solution in litre}} ;$$

$$\text{Number of gram equivalents} = \frac{\text{Weight of solute in grams}}{\text{Equivalent weight}}$$

$$\therefore \text{Normality} = \frac{\text{Weight of solute in grams}}{\text{Volume of solution in litre}} \times \frac{1}{\text{Equivalent weight}} \quad \therefore \text{Normality} = \frac{\text{Strength}}{\text{Equivalent weight}}$$

$$\therefore N = \frac{W}{V \times E} \quad \therefore W = N \times E \times V.$$

Note: Normality is dependent on volume, therefore, it changes with temperature.

5. **Normality of dilution:**

$$\begin{array}{ccc} \text{Concentrated solution} & & \text{Diluted solution} \\ N_1 V_1 & & N_2 V_2 \end{array}$$

6. **Normality of mixing:**

$$N_1 V_1 + N_2 V_2 + N_3 V_3 = N_R (V_1 + V_2 + V_3)$$

where N_R = Resultant normality, $V_1 + V_2 + V_3$ = Resultant volume after mixing.

7. **Relationship between normality and molarity of solution:**

$$\text{Normality} = \text{Molarity} \times \frac{\text{Molar mass}}{\text{Equivalent mass}} = \text{Molarity} \times n \quad \text{where } n = \frac{\text{Molar mass}}{\text{Equivalent mass}}$$

For acids, Normality = Molarity \times Basicity of acid. **For bases,** Normality = Molarity \times Acidity of base.

For oxidising / reducing agents, Normality = Molarity \times Change in oxidation number per molecule of reactant

Relation between mole fraction and molality:

8. **Relation between mole fraction and molality:**

$$\begin{aligned} X_A &= \frac{n_A}{n_A + n_B}, X_B = \frac{n_B}{n_A + n_B} ; & \frac{X_B}{X_A} &= \frac{n_B}{n_A} = \frac{W_B / M_B}{W_A / M_A} \Rightarrow \frac{X_B}{X_A} = \frac{W_B \cdot M_A}{M_B \cdot W_A} \\ \Rightarrow \frac{X_B}{X_A \cdot M_A} &= \frac{W_B}{M_B} \times \frac{1}{W_A} & \Rightarrow \frac{1000 X_B}{X_A M_A} &= \frac{1000 W_B}{M_B \cdot W_A} = m \Rightarrow \frac{1000 X_B}{(1 - X_B) \cdot M_A} = m \end{aligned}$$

Note: Mole fraction is independent of temperature of the solution as it is mass dependent only.

9. Expression relating molarity (M) and molality (m) of a solution:

Suppose we have 1000 ml of solution of molarity M and density d g/ml. 1000 ml solution has M moles of solutes i.e. MM_B grams of solute.

weight of solution = Volume \times density = 1000 dg

\therefore weight of solvent = weight of solution – weight of solute = $1000d - MM_B$.

\therefore $1000d - MM_B$ grass of solvent has M moles. $\therefore m = \frac{m}{100d - MM_B} \times 1000$

10. K_f and K_b are characteristics of solvent and respectively depend on its heat of fusion and heat of vaporisation as given below:

$$K_f = \frac{R \times M_1 \times T_f^2}{1000 \times \Delta_{\text{fus}} H} \quad M_1 = \text{Mol. wt of solvent} \quad ; \quad T_f = \text{freezing point of solvent (K)}$$

$$K_b = \frac{R \times M_1 \times T_b^2}{1000 \times \Delta_{\text{vap}} H} \quad R = \text{gas constant} \quad ; \quad T_b = \text{Boiling point of solvent (K)}$$

11. Van't Hoff factor is used to calculate the terms degree of dissociation or association of a substance in solution.

12. **Degree of dissociation:** It is defined as the fraction of total substance that undergo dissociation into ions.

$$\text{Degree of dissociation} = \frac{\text{No. of moles of the substance dissociated}}{\text{Total no. of moles of the substance taken}}$$

Suppose a molecule of an electrolyte gives 'm' ions after dissociation and α is the degree of dissociation, then

$$\alpha = \frac{i-1}{m-1}$$

13. **Degree of association:** It is defined as the fraction of total number of molecules which combine to form associated molecules.

$$\text{Degree of association} = \frac{\text{No. of moles of the substance associated}}{\text{Total no. of moles of substance taken}}$$

If suppose 'n' molecules of a solute associate to form the associated molecule and α is its degree of association,

$$\text{then } \alpha = \frac{i-1}{\frac{1}{n}-1}$$

14. **Azeotropes** are these liquid mixtures which boil at a constant temperature and distil over completely at the same temperature without change in composition.

- The components of an azeotrope cannot be separated by fractional distillation.
- Azeotropes arise due to very large deviations from Raoult's Law.
- The azeotropic mixture of ethanol-water contains approximately 95% by volume of ethanol.

15. There are two types of azeotropes.

a. **Minimum boiling point azeotropes:** These mixtures show a maximum in the vapour pressure curve and hence a minimum in the boiling point diagram, e.g., ethanol-water system. Exhibited by solutions showing positive deviation.

b. **Maximum boiling point azeotropes:** These mixtures show a minimum in the vapour pressure curve and hence a maximum in the boiling point diagram, e.g., HNO_3 - H_2O system. Exhibited by solutions showing negative deviation.

An azeotrope of HNO_3 and H_2O contains approximately 68% HNO_3 by mass and boils at 393 K.

39. Why is liquid ammonia bottle first cooled in ice before opening it?
40. Why does the use of a pressure cooker reduce cooking time?
41. 10 cc of a liquid A were mixed with 10 cc of liquid B. The volume of the resulting solution was found to be 19.9 cc. What do you conclude?
42. Two liquids A and B on mixing produce a warm solution which type of deviation from Raoult's Law does it show?
43. What happens if pressure greater than osmotic pressure is applied on the solution separated by a semi permeable membrane from the solvent?
44. What will happen to the elevation in boiling point of a solution if the weight of the solute dissolved is doubled but the weight of solvent taken halved?
45. Why it is advised to add ethylene glycol to water in a car radiator while driving in a hill station?
46. At the same temperature, hydrogen is more soluble in water than helium. Which of them will have a higher value of K_H and Why? (K_H = Henry's constant).
47. What do you mean by 10% w/w aqueous solution of Na_2CO_3 ?
48. What is the relation between normality and molarity of a given solution of H_2SO_4 ?
49. What type of liquids form ideal solutions?
50. What is the boiling point of an azeotrope of non-ideal solution showing positive deviations as compared to the boiling points of its components?
51. What are isotonic solutions? Give one example.
52. Define molal elevation constant or ebullioscopic constant.
53. Define molal depression constant or cryoscopic constant.
54. What is van't Hoff factor?
55. Why does water from the soil rise to the top of a tall tree?
56. Why NaCl solution freezes at lower temperature than water but boils at higher temperature than water?
57. Two liquids X and Y have boiling points 110°C and 130°C respectively. Which one of them has higher vapour pressure at 50°C ?
58. What freezes out first when a solution of common salt is cooled?
59. What is de-icing agent? How does it work?

PART II SHORT ANSWER QUESTIONS

1. Why there is an increase in vapour pressure when HgI_2 is added to the aqueous solution of KI?
2. Why is osmotic pressure considered to be a colligative property?
3. Will the elevation in boiling point be same if 0.1 mole of sodium chloride or 0.1 mole of sugar is dissolved in one litre of water?
4. CCl_4 and H_2O are immiscible whereas $\text{C}_2\text{H}_5\text{OH}$ and H_2O are miscible in all proportions. Correlate this behaviour with the molecular structures of the three compounds.
5. When fruits and vegetables that have dried are placed in water, they slowly swell and return to original form why? Would a temperature increase accelerate the process? Explain.
6. The van't Hoff factor of a solute in the solution is 0.5. What do you infer about nature of solute in the solution?
7. a. Name the factors which affect the solubility of a solute in a solvent.
b. Which one of the following has the lowest freezing point? 1 M urea solution, 1M Na_2SO_4 solution, 1 M NaCl
8. A deci molal solution of $\text{K}_4[\text{Fe}(\text{CN})_6]$ is 50% dissociated at 300 K. Calculate the osmotic pressure of solution. [$R = 0.0821 \text{ L atm K}^{-1} \text{ mol}^{-1}$]
9. At 25°C , the vapour pressure of pure water is 23.76 mm Hg and that of an aqueous dilute solution of urea is 22.98 mm Hg. Calculate the molality of this solution.
10. The vapour pressure of pure benzene at 25°C is 639.7 mm Hg and vapour pressure of a solution of a non-volatile solute is benzene at some temperature is 631.9 mm Hg. Calculate mole fraction of solute and molality of solution.
11. A solution containing 2.56g of sulphur in 100g of CS_2 gave a freezing point of lowering of 0.383 K. Calculate molecular formula of sulphur (K_f for $\text{CS}_2 = 3.83 \text{ K kg mol}^{-1}$, At. wt. of S = 32)
12. At 298 K, the vapour pressure of pure water is 23.75 mm Hg.

- a. At same temperature calculate vapour pressure over 10% aqueous solution of an organic compound whose molecular weight is 60 g mol^{-1} .
- b. What will be the osmotic pressure of this solution at 298 K? [Given $R = 0.082\text{ Latim K}^{-1}\text{ mol}^{-1}$].
13. An aqueous solution freezes at 272.4 K while pure water at 273K. Determine
- the molality of solution
 - boiling point of solution
- c. Lowering of vapour pressure of water at 298 K.
[Given $K_f = 1.86\text{ K kg mol}^{-1}$, $K_b = 0.512\text{ K mg mol}^{-1}$, vapour pressure of pure water is 23.756 mm Hg].
14. Explain why freezing point of a solvent is lowered on dissolving a non-volatile solute into it? Give on important application of the phenomenon of depression in freezing point.
15. With the help of suitable diagrams, illustrate the two types of non-ideal solutions.
16. Differentiate between molarity and molality of a solution. When and why is molality is preferred over molarity in handling solutions in chemistry.
17. What is molar concentration of solute particles in the human blood if the osmotic pressure is 7.2 atm at the body temperature of $37\text{ }^\circ\text{C}$? [$R = 0.0821\text{ L atm K}^{-1}\text{ mol}^{-1}$].
18. How much glucose must be dissolved in one litre of an aqueous solution so that its osmotic pressure is 2.57 atm at 300 K. [$R = 0.0821\text{ L atm K}^{-1}\text{ mol}^{-1}$].
19. Calculate the molar concentration of urea solution if it exerts an osmotic pressure of 2.45 atm at 300 K. [$R = 0.0821\text{ L atm K}^{-1}\text{ mol}^{-1}$].
20. Vapour pressure of pure water at $35\text{ }^\circ\text{C}$ is 31.82 mm Hg. When 27.0 g of solute is dissolved in 100 g of water (at same temperature), vapour pressure of solution thus formed is 30.95 mm Hg. Calculate molecular mass of the solute.
21. The vapour pressures of pure liquids A and B are 70 mm and 90mm Hg respectively at $25\text{ }^\circ\text{C}$. The mole fraction f_A in a solution of two is 0.3. Assuming that A and B form an ideal solution, calculate the partial pressure of each component is equilibrium with the solution.
22. a. Two liquids A and B boil at $145\text{ }^\circ\text{C}$ and $190\text{ }^\circ\text{C}$ respectively. Which of them has a higher vapour pressure at $80\text{ }^\circ\text{C}$?
b. Why is the vapour pressure of a solution of glucose in water lower than that of water?
23. Explain why are aquatic species are more comfortable in cold waters rather than warm waters?
24. What happens to the vapour pressure of a solution when
- a volatile solute dissolves in the liquid, and
 - the dissolved solute is non-volatile?
25. What are non-ideal solutions? Explain as to why non-ideal solutions deviate from Raoult's Law.
26. Is the solution of ethanol in water an ideal solution? Justify your answer.
27. Explain why a solution of ethyl alcohol and water cannot be separated into pure components by fractional distillation?
28. A mixture of ethanol and acetone shows positive deviation from Raoult's Law whereas that of chloroform and acetone shows negative deviation. Explain.
29. What is meant by positive and negative deviations from Raoult's Law and how is the sign of $\Delta_{\text{sol}} H$ related to positive and negative deviations from Raoult's Law?
30. A solution contains two volatile components A and B. What will be the relative compositions of the vapour and liquid if
- $P_A^\circ = P_B^\circ$
 - $P_A^\circ > P_B^\circ$
 - $P_A^\circ < P_B^\circ$
31. Draw a suitable labelled diagram to express the relationships, for ideal solutions of A and B, between vapour pressures and mole fractions of components at constant temperature.
32. State Raoult's Law. If ΔT is the elevation of boiling point of a solvent and m is the number of moles of solute per kg of solvent, what is the relationship between ΔT and m ?
33. Why does the boiling point of a solvent increase by the presence of solute is it? Write an expression showing the relationship between the elevation of boiling point and the molar mass of the solute.
34. Define osmotic pressure. How does it depend upon the temperature and atmospheric pressure?
35. What is reverse osmosis?
36. If 2g each of solutes A and B (Molecular mass of $A > B$) are dissolved separately in 20 g each of the same solvent C. Which will show greater lowering of vapour pressure and why?
37. After removing the outer shell of two eggs in dil. HCl, one is placed in distilled water and the other is placed in a saturated solution of NaCl. What will you observe and why?

35. This is because oil-water forces are not strong enough to overcome oil-oil and water-water forces.
36. Hydrated salts, i.e., contain water of crystallisation $\text{CuSO}_4 \cdot 5\text{H}_2\text{O}$.
37. This is because it reaches a state of equilibrium where rate of evaporation = rate of condensation.
38. This is because at lower temperature, the vapour pressure is low. Hence, lesser vapours of tear producing chemicals are produced.
39. At room temperature, the vapour pressure of liquid ammonia is very high. On cooling, vapour pressure decreases. Hence, the liquid ammonia will not splash out.
40. The weight over the lid does not allow the steam to go out. As a result, pressure inside the cooker is high. Higher the external pressure higher is the boiling point and faster is the cooking.
41. Decrease in volume means stronger intermolecular forces of attraction on mixing. This implies that the solution shows negative deviation from Raoult's Law.
42. Warming up of a solution means that the process of mixing is exothermic, i.e., $\Delta H_{\text{mixing}} = \text{negative}$. This implies that the solution shows a negative deviation.
43. Reverse osmosis, i.e., net flow of the solvent is from solution to solvent.
44. The elevation in boiling point will become four times because $\Delta T_b = K_b = \frac{W_2 \cdot 1000}{M_2 \cdot W_1}$
45. It is done to lower the freezing point of water so that it does not freeze.
46. As H_2 is more soluble than helium, H_2 will have lower value of K_H than that of helium.
47. It means that 10g of Na_2CO_3 are present in 100g of the solution.
48. Normality = $2 \times$ Molarity.
49. Liquids having similar structures and polarities.
50. The boiling point of such an azeotrope is lower than that of its components.
51. Solution having same osmotic pressure is called isotonic solutions, e.g., 0.1 M glucose and 0.1 M sucrose solutions.
52. The elevation in boiling point that takes place when molality of the solution is unity.
53. The depression in freezing point that takes place when the molality of the solution is unity.
54. It is the ratio of the observed colligative property to the theoretical value.
55. Due to osmosis through the roots because root cell walls are made up of semipermeable membrane.
56. When a solute is dissolved in a solvent the vapour pressure decreases. As a result, the solution boils at a higher temperature while solvent freezes at a lower temperature.
57. Lower the boiling point, more volatile it is. Hence, liquid X will have higher vapour pressure at 50°C .
58. Water as ice.
59. Common salt is called de-icing agent because it lowers the freezing point of water to such an extent that it does not freeze to form ice. Hence, it is used to clear snow from roads.

PART II SHORT ANSWER QUESTIONS

1. When HgI_2 is mixed with KI (aq), a complex K_2HgI_4 is formed and thus the number of particles in the solution are decreased.



Due to the decrease in number of particles, vapour pressure is increased.

2. Osmotic pressure, $\pi = \frac{n}{V} RT$. It is clear from the relation that osmotic pressure, π depends only on the number of moles of solute present in a definite volume of solution. Hence, it is a colligative property.
3. The elevation in boiling point of 0.1 mole of NaCl and 0.1 mole of sugar dissolved in water will not be same. Elevation in boiling point is a colligative property and depends upon the number of solute particles. NaCl is ionic and gives more number of particles due to ionisation than sugar which consists of molecules.
4. CCl_4 is a non-polar compound, whereas H_2O is a polar compound having hydrogen bonding. When CCl_4 is mixed with H_2O , CCl_4 is not able to break the hydrogen bonding of H_2O and hence remains immiscible.

However, both C_2H_5OH and H_2O are polar compounds and form hydrogen bonding. When C_2H_5OH is mixed with H_2O , the hydrogen bonding between the two takes place and thus mixing occurs.

5. It is due to osmosis that the dried fruits and vegetables slowly swell when placed in contact with water. The outer layer of the fruits and vegetable (i.e., cell wall) acts as a semi-permeable membrane. Yes, with a increase in temperature, the osmosis accelerates as the osmotic pressure of a solution increases with increase in temperature, $\pi \propto T$.

6. van't Hoff factor, $i = \frac{\text{Number of particle of solute in solution}}{\text{Number of solute molecules in normal state}} = \frac{\text{Observed colligative property}}{\text{Number colligative property}}$

Since $i = 0.5$, it means that the number of particle (ions or molecules) of solute in solution is less than that in normal state. It indicates that the solute molecules undergo association.

7. a. Factors affecting the solubility of a solute are:
 (i) Nature of solute and solvent (ii) Temperature and pressure
 b. $1M Na_2SO_4$ has lowest freezing point because the number of effective solute particles are maximum as one molecules dissociate into three ions.

8. Concentration, $C = \frac{n_B}{V} = 0.1 M$; As degree of dissociation is 50%, $\alpha = 0.5$

$T = 300 K$ $K_4 [Fe(CN)_6] \rightleftharpoons 4K^+ + [Fe(CN)_6]^{4-} \therefore n = 5$, van't Hoff factor 'i' can be calculated by relation,

$$\text{degree of dissociation} = \frac{i-1}{n-1} \therefore 0.5 = \frac{i-1}{5-1} ; 0.5 = \frac{i-1}{4} ; i-1 = 2$$

$$i = 3 ; \pi = iCRT = 3 \times 0.1 \times 0.0821 \times 300 = 7.389 \text{ atm.}$$

9. $P_A^\circ = 23.75 \text{ mm}$; $P_A = 22.98 \text{ mm}$; Let X_B mole fraction of solute

According to Raoult's Law, $\frac{P_A^\circ - P_A}{P_A^\circ} = X_B \therefore X_B = \frac{23.76 - 22.98}{23.76} = \frac{0.78}{23.76} = 0.0328$

For dilute solutions, $X_B = n_B/n_A$ or $n_B = n_A X_B$

If we consider 1 kg of water, then n_B becomes number of moles of solute per kg of solvent and thus molality of

solution, $\therefore n_B = \frac{1000}{18} \times 0.0328 = 55.5 \times 0.0328 = 1.82 \text{ mol/kg of solvent.}$

10. Using relation, $X_B = \frac{P_A^\circ - P_A}{P_A^\circ} = X_B$

$$X_B = \frac{639.7 - 631.9}{639.7} = 0.0122 ; X_{\text{solute}} = \frac{n_{\text{solute}}}{n_{\text{solute}} + n_{\text{solvent}}} ; X_{\text{solute}} = \frac{n_B}{n_B + \frac{1000}{78}} = \frac{n_B}{n_B + 12.82}$$

{when are consider weight of solvent equal to 1000 g then n_B obtained is molality}

$$0.0122 = \frac{n_B}{n_B + 12.82} ; n_B = 0.0122n_B + 12.82 \times 0.0122$$

$$(1 - 0.0122) n_B = 12.82 \times 0.0122 = 0.1564 \therefore n_B = \frac{0.1564}{0.9878} = 0.158 \text{ moles/kg of benzene.}$$

11. Using relation, $\Delta T_f = K_f m = K_f \frac{W_B \times 1000}{M_B \times W_A} \therefore M_B = \frac{3.82 \times 2.56 \times 1000}{0.383 \times 100} = 256 \text{ g mol}^{-1}$

Atomic weight of sulphur = 32 ; \therefore No. of atoms in one molecule of sulphur = $\frac{\text{Mol. wt}}{\text{At. wt}} = \frac{256}{32} = 8$.

The molecular formula of sulphur is S_8

12. Let there is 100 g of solution i.e., 10 g of organic compound is 90 g of water

$$n_B = \frac{W_B}{M_B} = \frac{10}{60} = \frac{1}{6}; \quad n_A = \frac{W_A}{M_A} = \frac{90}{18} = 5.$$

$$\frac{P_A^\circ - P_A}{P_A^\circ} = X_B; \quad \frac{n_B}{n_A + n_B} = \frac{1/6}{5 + 1/6} = \frac{1}{31} \quad \frac{23.75 - P_A}{23.75} = \frac{1}{31}; \quad 23.75 - P_A = \frac{23.75}{31} = 0.766 \Rightarrow P_A = 22.98 \text{ mm Hg.}$$

b. Osmotic pressure, $\pi = \frac{n_B}{V} RT = \frac{1 \times 0.082 \times 298}{6 \times 0.1}; \quad \pi = 40.73 \text{ atm.}$

13. a. $\Delta T_f = 273 - 272.4 = 0.6 \text{ K} \quad \Delta T_f = K_f m \quad \therefore \text{molality, } m = \frac{\Delta T_f}{K_f} = \frac{0.6}{1.86} = 0.322 \text{ mol/kg.}$

b. $\Delta T_b = K_b \times m = 0.512 \times 0.322 = 0.165 \text{ K.}$ Boiling point of solution = $373 + \Delta T_b = 373 + 0.165 \text{ K} = 373.165 \text{ K}$

c. $\frac{P_A^\circ - P_A}{P_A^\circ} = X_B = \frac{n_B}{n_A + n_B}$

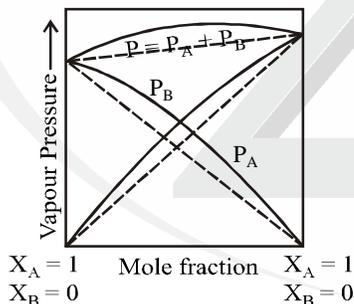
Moles of solute per kg of solvent = $n_A = 0.322$; Moles of solvent per kg of solvent = $n_B = \frac{1000}{18} = 55.55$

Mole fraction of solute, $X_B = \frac{0.322}{55.55 + 0.322} = 0.0057 \quad \therefore \text{Lowering of vapour pressure,}$

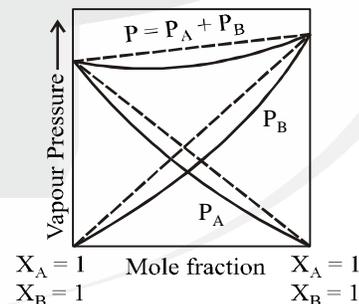
$$P_A^\circ - P_A = P_A^\circ X_B = 23.756 \times 0.0057 = 0.137 \text{ mm Hg.}$$

14. Lowering of vapour pressure is the basic cause of depression in freezing point. Since the vapour pressure of a solution is lower than that of pure solvent, the temperature of freezing of the solution is lower than that of pure solvent. Liquid freezes at a vapour pressure at which solid form can also exist with in equilibrium, i.e., at freezing point there exists an equilibrium between liquid phase and solid phase of solvent.

15. The use of freezing mixtures (salts + ice) in making of kulfis, use of antifreeze into water especially in very cold regions, determination of molar mass, etc., are important applications of depression in freezing point.



A vapour pressure graph showing a positive deviation (solid lines) from ideal behaviour (dotted lines).



A vapour pressure graph showing a negative deviation (solid lines) from ideal behaviour (dotted lines).

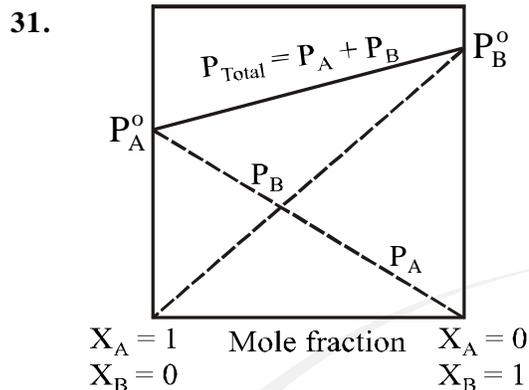
16. Molarity is the number of moles of solute dissolved per litre of solution. $M = \frac{n_B}{V \text{ (in litres)}}$

Molality is the number of moles of solute dissolved per kg of solvent. $m = \frac{n_B}{W_B \text{ (in kg)}}$

Molality does not change with temperature whereas molarity change with temperature. Therefore, molality is used in study of elevation in boiling point, depression in freezing point and in very accurate analytical measurements involving variation of temperature.

Negative deviation from Raoult's Law is exhibited when the measured vapour pressure is lower than the predicted vapour pressure. It occurs when A – B interactions are stronger than those between A – A and B – B interactions. $\Delta_{\text{Sol}} H$ is $-ve$ i.e., < 0 .

30. a. $P_A^\circ = P_B^\circ$. It means that the composition of A and B will be same in both the liquid and the vapour phase $P_A^\circ > P_B^\circ$. It means that the vapour phase is richer in A component.
- b. $P_A^\circ < P_B^\circ$. It means that the vapour phase is richer in B component whereas the liquid phase is richer in A component.



32. According to Raoult's Law, the vapour pressure of a solution containing a non-volatile solution is directly proportional to the mole fraction of the solvent (X_A), $P \propto X_A$. $P = P^\circ X_A$, where $P^\circ =$ Vapour pressure of pure solvent.

If the solution consists of two volatile liquids, then Raoult's Law in $P_A = P_A^\circ X_A$ and $P_B = P_B^\circ X_B$. And the total vapour pressure of the solution is equal to the sum of the partial vapour pressure of each component.

$$P = P_A + P_B = P_A^\circ X_A + P_B^\circ X_B \quad \text{Relation between } \Delta T \text{ and } m, \Delta T \propto m$$

$$\Delta T = K_b m \quad \text{where } K_b \text{ is a proportionality constant called molal elevation constant.}$$

33. The boiling point of a liquid is the temperature at which the vapour pressure of the liquid becomes equal to the atmospheric pressure. When a non-volatile solute is dissolved in a solvent, the vapour pressure of the solvent is decreased, i.e., the temperature at which the vapour pressure of the solution will equal the atmospheric pressure will be higher than the temperature at which the vapour pressure of the pure solvent equals the atmospheric pressure. In other words, the boiling point of a solvent increases by the presence of a solute in it.

Relationship between the elevation of boiling point and the molal mass of the solute, $\Delta T_b = K_b m = \frac{K_b W_B 1000}{M_B W_A}$

34. Osmotic pressure (π) is the pressure which must be applied to the solution side (more concentrated solution) to just prevent the passage of pure solvent into it through a semipermeable membrane. $\pi = CRT = \frac{n_B}{V} RT$

As can be seen from the above expression, osmotic pressure, π is directly proportional to the temperature on the Kelvin, scale, i.e., the osmotic pressure increases with rise in temperature.

Osmotic pressure is independent of atmospheric pressure.

35. Consider a solution separated from the pure solvent by a semipermeable membrane. If the pressure applied to the solution side is more than the osmotic pressure, the solvent will flow from the solution to the solvent side. This phenomenon is called reverse osmosis.

36. For dilute solutions, $\frac{P^\circ - P_s}{P^\circ} = \frac{W_2 M_1}{W_1 M_2}$; $\frac{\Delta P}{P^\circ} = \frac{W_2 M_1}{W_1 M_2}$

For same, P° , i.e., P° constant and M_1 is also constant. $W_2 = W_A = W_B = 2g$; $W_1 = W_C = 20g$

Hence $\frac{\Delta P_A}{\Delta P_B} = \frac{M_B}{M_A}$. As $M_A > M_B$, therefore, $\Delta P_B > \Delta P_A$. It means B will show greater lowering of vapour pressure.

37. Egg in water will swell while egg in NaCl solution will shrink. This is because as a result of osmosis, the net flow of solvent is from less concentrated to more concentrated solution.
38. (i) They will shrink due to plasmolysis.
(ii) They will swell and may even burst.
RBC's are isotonic with 0.9% NaCl solution.
39. van't Hoff Factor (i) for NaCl is 2 ; van't Hoff Factor (i) for BaCl₂ is 3.

$$\frac{(\Delta T_f)_{\text{NaCl}}}{(\Delta T_f)_{\text{BaCl}_2}} = \frac{2}{3} \quad ; \quad \therefore (\Delta T_f)_{\text{BaCl}_2} = \frac{3}{2} \times (-2^\circ\text{C}) \quad \therefore (\Delta T_f)_{\text{BaCl}_2} = -3^\circ\text{C}.$$

40. When NaCl which is non-volatile is dissolved in water, vapour pressure of water decreases because some of the solvent molecules on the surface are replaced by the molecules of the solute which are non-volatile. The solution has to be heated more to make vapour pressure equal to the external pressure. Hence, boiling point is increased.

PART III LONG ANSWER QUESTIONS

1. Glucose when dissolved in water does not associate or dissociate in water, so its experimental molecular weight is equal to its theoretical molecular weight whereas KCl is a strong electrolyte, each molecule of KCl dissociates in water to give two ions (particles), i.e., $\text{KCl} \rightleftharpoons \text{K}^+ + \text{Cl}^-$.

Hence, its depression in freezing point found experimentally is double its calculated value, i.e., its van't Hoff factor = 2.

As, colligative property $\propto \frac{1}{\text{Molecular Mass}}$, therefore experimental molecular mass is half its theoretical value.

2. The external pressure applied to solution in order to stop the osmosis of solvent into solution separated by semipermeable membrane is called osmotic pressure.

$$\pi = CRT$$

Osmotic pressure is a colligative property and depends upon the number of particles of solute in solution. Glucose and sucrose are non-electrolytes, therefore, they do not dissociate or associate in solution while NaCl is an electrolyte and on dissolving in water it dissociates to give two ions:



$$\pi = i \left(\frac{n}{V} \right) RT = i CRT$$

- a. For sucrose, $i = 1$ (as it neither dissociates nor associates in solution)

$$C = \frac{34.2}{342} = 0.1 \text{ moles/litre} \quad \therefore \pi_{\text{sucrose}} = 1 \times 0.1 \times RT = 0.1 RT \text{ atm.}$$

- b. For glucose, $i = 1$ (as it neither dissociation nor associates in solution) $C = \frac{90}{180} = 0.5 \text{ moles/litre}$

$$\therefore \pi_{\text{glucose}} = 1 \times 0.5 \times RT = 0.5 RT \text{ atm.}$$

- c. For NaCl, $i = 2$ (as it dissociates in solution to give 2 ions) $C = \frac{5.85}{585} = 0.1 \text{ moles/litre}$

$$\pi_{\text{NaCl}} = 2 \times 0.1 \times RT = 0.2 RT \text{ atm}$$

Thus, the increasing order of osmotic pressure of the above solutions is as follows: Sucrose < NaCl < Glucose

3. a. Refer to brief resume
- b. Vapour pressure of solution will be less than expected from Raoult's law. Values of ΔH_{sol} and ΔV_{sol} will also be less than zero i.e., heat is released and there is contraction in volume.
- c. When solvent contains solute particles, the effective surface area available to solvent molecules to escape decreases. A part of surface area gets occupied by non-volatile solute particles.
- d. Liquid P with lower boiling point high higher partial vapour pressure.

4. a

Ideal solutions	Non-ideal solutions
(i) A – B interactions are very much similar to A – A and B – B interactions.	(i) A – B interactions are very much different (either stronger or weaker) from A – A and B – B interactions.
(ii) There is no change in volume in the formation of solution, i.e., $\Delta V_{\text{mix}} = 0$.	(ii) The volume of solution is either less or more than the total volume of components, i.e., $\Delta V_{\text{mix}} \neq 0$.
(iii) No heat change takes place, i.e., $\Delta H_{\text{mix}} = 0$.	(iii) Enthalpy change takes place, i.e., $\Delta H_{\text{mix}} \neq 0$. Heat is evolved or absorbed in the process of solution formation.
(iv) They obey Raoult's Law at all temperature and concentrations.	(iv) They do not obey Raoult's Law.

b. By Raoult's Law, $P_A = P_A^\circ X_A$ and $P_B = P_B^\circ X_B$

Total vapour pressure, i.e., $P = P_A + P_B = P_A^\circ X_A + P_B^\circ X_B$

We know that $X_A = 1 - X_B$; $P_A = P_A^\circ (1 - X_B) + P_B^\circ X_B = P_A^\circ - P_A^\circ X_B + P_B^\circ X_B = P_A^\circ + (P_B^\circ - P_A^\circ) X_B$.

c. Consider 1 litre of pure water, i.e., 1000 mL

Weight of 1000 mL of water = Volume \times Density = $1000 \times 1 = 1000$ g.

Moles of water = $\frac{1000}{18} = 55.55$ moles. Hence, 55.55 moles of water are present in one litre of water.

\therefore Molarity of water = 55.55 M.

5. a. In a solution, sum of mole fractions of all components is unity.

$\therefore X_A + X_B + X_C = 1$; $\therefore X_B = 1 - (X_A + X_C) = 1 - (0.5 + 0.2) = 0.3$.

b. $M = \frac{n_B}{V \text{ in litres}}$ and $m = \frac{n_B}{W \text{ in kg}}$

Where M is molarity and m is molality. M and m will be equal if 1 litre of solution has mass of 1 kg.

This is generally true in case of very dilute aqueous solutions at room temperature when density of solution can be taken as 1 g cm^{-3} .

c. Total volume of solution = $V = 100 + 100 = 200 \text{ mL} = 0.2 \text{ L}$

After mixing of two solutions, 6g of urea is present in 200 mL solution.

$\therefore \pi_1 = \frac{n_B}{V} RT = \frac{6/60}{0.2} \times \frac{0.0821 \times 300}{1} = 12.315 \text{ atm}$

(When molar mass of urea $\text{NH}_2\text{CONH}_2 = 2 \times 14 + 12 + 16 + 4 \times 1 = 60$)

Similarly, 18g of glucose ($\text{C}_6\text{H}_{12}\text{O}_6$) is present in 200 ml solution.

Osmotic pressure due to glucose,

$$\pi_2 = \frac{n_B}{V} RT = \frac{18 \times 0.0821 \times 300}{180 \times 0.2} \text{ atm} = 12.315 \text{ atm}$$

The two solutes behave independently and total osmotic pressure is the sum of two.

Osmotic pressure of mixture, $\pi = \pi_1 + \pi_2 = 12.315 + 12.315 = 24.630 \text{ atm}$.

PART IV SKILL ANALYSER

1. Henry's Law states that the solubility of a gas in a liquid at a given temperature is directly proportional to the partial pressure of the gas.
2. The solubility of a gas in a liquid decreases with increase in temperature.
3. This is because the value of osmotic pressure of a solution depends upon the number of particles of solute per litre of solution.
4. The molarity of a solution is the number of moles of solute present in one litre of the solution.

The molarity of a solution changes, with temperature because the volume of the solution changes with change in temperature.

5. Aquatic species get their requirement of oxygen from water containing dissolved oxygen.
Since the solubility of a gas in liquid decreases with rise in temperature (1 mark) warm water dissolve less amount of oxygen as compared to cold water. Hence, aquatic species are more comfortable in cold water rather than warm water.
6. (1) Plants absorb water from the soil through their roots due to osmosis.
(2) In animals water moves into different parts of body due to osmosis.
(3) Movements in plants like opening and closing of flowers etc., are regulated by osmosis.
7. (i) No. of moles of heptane (C_7H_{10}) in the solution

$$= \frac{\text{Mass}}{\text{Molar Mass}} = \frac{25}{(7 \times 12 + 1 \times 16)} = \frac{25}{100} = 0.25 \text{ mol}$$

$$\text{No. of moles of octane } (C_8H_{18}) \text{ in the solution} = \frac{\text{Mass}}{\text{Molar Mass}} = \frac{35}{8 \times 12 + 1 \times 18} = \frac{35}{114} = 0.307 \text{ mol}$$

$$\text{Mole fraction of heptane} = \frac{0.25}{0.25 + 0.307} = 0.4488 \quad ; \quad \text{Mole fraction of octane} = \frac{0.307}{0.25 + 0.307} = 0.5512$$

$$P_{\text{Heptane}} = P^\circ_{\text{Heptane}} X_{\text{Heptane}} = 105.2 \times 0.4488 = 47.2 \quad ; \quad P_{\text{Octane}} = P^\circ_{\text{Octane}} X_{\text{Octane}} = 46.8 \times 0.5512 = 25.8$$

$$\text{Vapour pressure of a mixture} = 47.2 + 25.8 = 73.0 \text{ kPa}$$

$$\text{We know that } 1 \text{ bar} = 100 \text{ kPa} \quad \therefore 73.0 \text{ kPa} = \frac{1 \text{ bar}}{100 \text{ kPa}} \times 73.0 \text{ kPa} = 0.73$$

(ii) When HgI_2 is mixed with KI (aq), a complex K_2HgI_4 is formed and thus the number of particles in the solution are decreased.



Due to the decrease in number of particles, vapour pressure is increased.